

# Accumulation of nonlinear noise in coherent communication lines without dispersion compensation



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## ABSTRACT

The nature of accumulation of nonlinear noise in multi-span communication lines with optical amplifiers without dispersion compensation was investigated experimentally and theoretically. It has been established that the dependence of nonlinear noise power on the number of spans is described by a power function with an exponent greater than 1. It has also been established that the nonlinear noise power generated in one span is practically independent on the amount of dispersion accumulated before this span for the values of accumulated dispersion more than 2 ns/nm. Since the noise power generated in one span does not depend on number of this span, in order to describe the superlinear dependence of total noise on number of spans we can assume that noises generated in different spans are correlated.

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## 1. Introduction

An important characteristic of the modern coherent communication systems is their ability to operate without physical compensation of chromatic dispersion. Linear distortions caused by chromatic dispersion and polarization mode dispersion are effectively eliminated in coherent communication lines during digital signal processing on the receiver. Therefore the main sources of distortion in coherent lines are nonlinear effects.

In order to compensate nonlinear distortions effectively it is necessary to investigate the nature of their accumulation during the propagation of optical signal along a fiber link. It was shown experimentally and theoretically in a number of recent works that nonlinear distortions in coherent communication lines without dispersion compensation can be regarded as additional nonlinear noise that is generated due to nonlinear interaction of symbols of a transmitted signal.

The concept of nonlinear noise was first introduced in early 1990s in the original paper [1]. Closed-form analytical expressions for the nonlinear interaction between spectral components of signals were derived in [2], as well as analytical expressions for spectral density of nonlinear noise power. The same expressions were also successfully used to describe nonlinear interaction of signal and amplified spontaneous emission (ASE) noise [3].

This nonlinear noise can be described as a Gaussian noise [4–19], at least in dispersion uncompensated (DU) coherent systems. Gaussian nature of the nonlinear interference (NLI) noise fields is conditioned by Gaussian distribution of the information sampled signal [4–6,14–16]. The Gaussian noise (GN) model of NLI noise is attractive for practical use because it allows elementary system optimization rules based on the signal to noise ratio [17,18]. Several analytical models for performance evaluation and design of such systems have been proposed [5–9,19]. An alternative time-domain theory predicts that a large fraction of nonlinear noise can be characterized as phase noise [20].

Recent experimental and theoretical researches have shown that the nonlinear noise power in a long multi-span line increases with the number of spans a bit faster than linearly [7,11]. Two mechanisms were suggested in [11] to explain the superlinear dependence of accumulated nonlinear noise power on communication line length: a) correlation of noises that are generated in different spans, and b) increase of nonlinear noise power generated in a span with increasing of accumulated dispersion. The latter hypothesis was investigated in [11] and its confirmations were reported.

In our work we have investigated experimentally and numerically the increase of nonlinear noise power with increasing of channel power and number of spans, as well as the dependence of nonlinear noise power generated in a span on accumulated dispersion. It was shown that the dependence of nonlinear noise power on the number of spans is described by a power function

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with an exponent greater than 1. But it has also been established that the nonlinear noise power generated in one span is practically independent on the amount of dispersion accumulated before this span for the values of accumulated dispersion more than 2 ns/nm. This result contradicts the results reported in [11].

Thus we can suppose that the possible reason for superlinear dependence of nonlinear noise power on the communication line length is a correlation of noises that are generated in different spans. This hypothesis needs further research.

## 2. Experimental setup

The experimental assembly that is used for research of impact of the accumulated dispersion on a value of non-linear distortions is schematically shown on Fig. 1. The communication line model contains several spans; the quantity of spans can be varied from 1 to 40. Each span consists of 100 km of SSMF fiber (G.652) and an EDFA that fully compensates attenuation in the fiber.

An optical transmitter converts an electrical signal into an optical signal with NRZ DP-QPSK modulation format. We use commercially available transponder based on full C-band tunable external cavity lasers (ECL) and Mach-Zehnder quadrature modulator [21]. The symbol rate is 30 GBaud / s and the bit rate is 120 Gbit / s (each symbol bears 4 bits).

All the internal parameters of the optical module are tuned automatically. A master laser of transmitter and a reference laser of receiver are full C-band tunable external cavity lasers (ECL) with approximately 100 kHz width of the emission band. A more detailed description of the transmitter can be found in [22–24].

The emission from the transmitter with a wavelength of 1549.32 nm is sent to input of a booster (power amplifier) via multiplexer (MUX). Then it passes through a tunable dispersion compensator (TDC) and enters the input of a communication line model. At the output of the line, a little part of the emission is sent to an optical spectrum analyzer (OSA) using the optical coupler (splitter). An additional noise can be injected in the line using an amplified spontaneous emission (ASE) source; the noise level can be tuned using a variable optical attenuator (VOA). The main part of the signal is transferred from the output of the line to demultiplexer (DEMUX) and then (after amplification in pre-amplifier) to a receiving part of the transponder. The transponder contains an intrinsic pseudorandom signal generator and a tool for measurement of bit error ratio (BER) before FEC error correction.

The tunable dispersion compensator (TDC) allows user to vary smoothly a value of accumulated dispersion at the input of the line in the range from -1000 ps/nm to +1000 ps/nm. Each span adds 1700 ps/nm, so the dispersion at the input of the  $N$ th span can be varied in the range from  $(1700N - 2700)$  ps/nm to  $(1700N - 700)$  ps/nm.

## 3. Theoretical analysis

In accordance with the model of nonlinear noise [4], nonlinear distortions can be regarded as nonlinear noise  $P_{NL}$  that is combined additively with the noise of amplified spontaneous emission  $P_{ASE}$  (ASE noise):

$$P_{\Sigma} = P_{NL} + P_{ASE} \quad (1)$$

where  $P_{\Sigma}$  – total noise.

Since the noise power and the signal power undergo amplifications and attenuations during their propagation in the communication line, it is more convenient to use in calculations not the absolute values of powers, but their ratios (optical signal-to-noise ratio, OSNR):  $OSNR_{ASE} = P_{\Sigma}/P_{ASE}$ ,  $OSNR_{NL} = P_{\Sigma}/P_{NL}$ ,  $OSNR_{BER} = P_{\Sigma}/P_{\Sigma}$  [7].

Using the OSNR notation, the formula (1) can be rewritten as follows:

$$OSNR_{BER}^{-1} = OSNR_{NL}^{-1} + OSNR_{ASE}^{-1} \quad (2)$$

The value  $OSNR_{BER}$  is related with a bit error ratio BER and a quality factor  $Q$  by fundamental relationships:

$$BER = \frac{1}{2} \operatorname{erfc}\left(\frac{Q}{\sqrt{2}}\right) \quad (3)$$

$$Q = \sqrt{\frac{B_0}{B_E} OSNR_{BER}} \quad (4)$$

where  $B_0/B_E$  – the ratio of optical and electrical bandwidths.

In real line, we can measure  $OSNR_{ASE}$  using OSA, and we can calculate  $OSNR_{BER}$  using the waterfall curve of transponder (which represents the dependence of BER before FEC on OSNR measured in a back-to-back scheme). Thus we can calculate  $OSNR_{NL}$  using (2) and nonlinear coefficient  $\eta_{NL}$  that is defined as follows:

$$\frac{1}{OSNR_{NL}} = \eta_{NL} P_{\Sigma}^2 \quad (5)$$

In order to take into account the technical noises of the transmitter and the receiver, it was offered in [4] to add in (2) an additional member:

$$OSNR_{BER}^{-1} = OSNR_{NL}^{-1} + OSNR_{ASE}^{-1} + X_T \quad (6)$$

The additional member in the expression allows us to take into consideration the noises of technical origin of any nature. The  $X_T$  can be calculated during measurements of transponder's characteristics in a back-to-back scheme, where nonlinear effects can be neglected [4]. As noises in the line decrease, the BER approaches not to null value but to some minimal level – error floor (due to electrical noises of receiver and other technical noises). The intersection of experimental error floor and theoretical  $BER(OSNR)$  curve (2–4) defines the  $X_T$  value.

The formula (6) can be re written as follows:

$$P_{\Sigma} = P_{NL} + P_{ASE} + X_T P_{\Sigma} \quad (7)$$

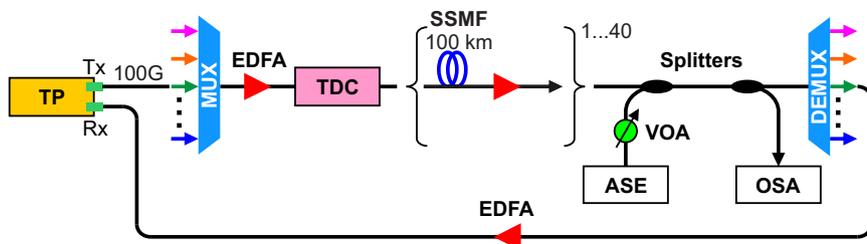


Fig. 1. Experimental setup. TDC – tunable dispersion compensator (from -1000 ps/nm to +1000 ps/nm); TP – transponder with a tool for measurement of BER before FEC.

Thus the nonlinear noise power  $P_{NL}$  can be calculated using (7):

$$P_{NL} = P_{\Sigma} - P_{ASE} - X_T P_{\Sigma} \tag{8}$$

where  $P_{ASE} = P_{\Sigma} / OSNR_{ASE}$  and  $P_{\Sigma} = P_{\Sigma} / OSNR_{BER}$ .

### 4. Experimental results

#### 4.1. Dependence of nonlinear coefficient on the number of spans

The nonlinear noise power in multi-span lines is proportional to third degree of signal power with a factor of proportionality  $\eta_{NL}$  (5). So if we know the nonlinear noise, we can find  $\eta_{NL}$ .

To calculate  $\eta_{NL}$  for the whole line, we set an equal signal power at inputs of all spans and then vary the signal power in some range. In our experiment, we used the range 0–5 dBm.

OSNR is measured for different input signal powers, and the resulting graph of dependence allows both to check the (5) rule and to calculate the  $\eta_{NL}$ .

Fig. 2 shows the dependence of nonlinear coefficient  $\eta_{NL}$  for the line on number of spans in the line. The line contains  $N$  spans (100 km of SSMF fiber each).

The experimental dependence of  $\eta_{NL}$  on  $N$  (for large  $N$ ) can be approximated with a power function of the following form:  $\eta_{NL} = \zeta N^{1+\epsilon}$ .

Experimental data for  $N \leq 20$  have less accuracy than for  $N > 20$ . The possible reason for the lower quality of experimental data for short lines is an incorrect choice of the range of the signal power variation. To increase the accuracy of experiment, the range of signal power variation should be adjusted depending on number of spans in the tested line. The signal power that maximizes the OSNR margin of the line should be chosen as a central point of the range (the maximal value is limited by the line operability, and the minimal value is approximately symmetrical to the maximal value about the central point). For example, the range should be 8–15 dBm for 1-span line, and 0–5 dBm for 40-span line. In our case we used the range 0–5 dBm for all lines that resulted in less accuracy of experimental data for short lines. Thus we use only data for  $N > 20$  to estimate parameters of the dependence function.

We can suppose that the factor of proportionality  $\zeta$  equals to the saturation level of nonlinear coefficient of a single span (see

below, chapter 4.2). This value was calculated numerically and determined experimentally:  $\eta_0 = 14.2 \times 10^{-5} \text{ mW}^{-2}$ . In this case the best approximation of experimental data with the power function is achieved when  $\epsilon = 0, 15$  (coefficient of determination  $R^2 = 0, 9841$ ). The resulting approximation is shown on Fig. 2.

Another possible approximation of the same set of experimental data could be made by variation of the both parameters simultaneously ( $\zeta$  and  $\epsilon$ ). In this case the following parameters provide the best approximation of experimental data with the power function:  $\zeta = 11.1 \times 10^{-5} \text{ mW}^{-2}$  and  $\epsilon = 0, 22$  (coefficient of determination  $R^2 = 0, 9875$ ). The discrepancy with the previous method can be regarded as an indirect estimation of the accuracy of calculation of parameters  $\zeta$  and  $\epsilon$ .

Thus the superlinear dependence of nonlinear coefficient of the line on the number of spans is confirmed, as well as in [11].

The experimental assembly allows us also to investigate the effect of composition of nonlinear noises in arbitrary sets of spans. However we were failed to observe the effect of superlinear accumulation of total noise if the number of spans in nonlinear mode is small. We suppose that the effect is below our experimental precision in this case.

#### 4.2. Dependence of nonlinearity on accumulated dispersion

A dependence of nonlinear noise power that is generated in one span on accumulated dispersion (in the range from  $-1000 \text{ ps/nm}$  to  $+26500 \text{ ps/nm}$ ) was measured as follows. A signal power was set to high value (+13 dBm) at the input of the tested span to provide nonlinear mode in this span. At inputs of all other spans a signal power was set to low values ( $-2 \text{ dBm}$ ) to provide linear mode. A BER before FEC was measured using internal tool of the transponder. Based on the measured value of BER before FEC and the waterfall curve of the transponder we have calculated the nonlinear noise power using (8) and then a nonlinear coefficient  $\eta_{NL}$  for the tested span using (5).

The dependence of BER on amount of dispersion accumulated before the tested span that operates in nonlinear mode (signal power +13 dBm) is shown on Fig. 3.

The experiment shows that BER before FEC (and nonlinear noise accordingly) increases with the increase of accumulated dispersion only before the value of accumulated dispersion

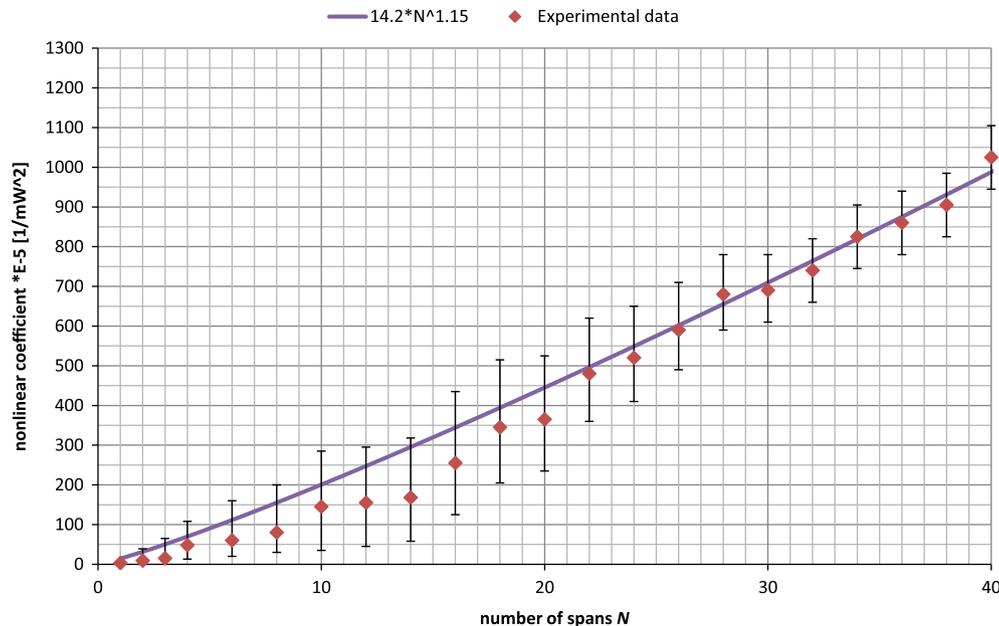


Fig. 2. Experimental setup. Dependence of nonlinear coefficient on the number of spans  $N$ .

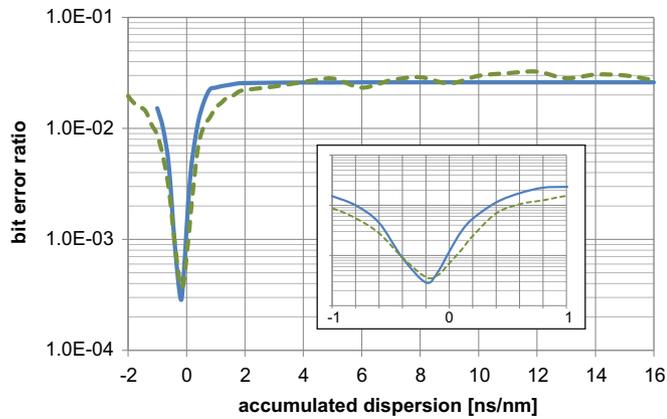


Fig. 3. Dependence of BER before FEC on accumulated dispersion. Solid line: experimental data (see Section 2). Dashed line: computer simulation (see Section 5).

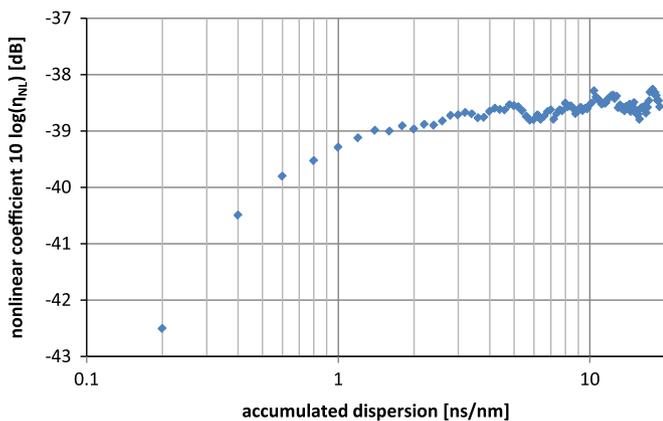


Fig. 4. Dependence of nonlinearity coefficient (in logarithmic units) for one span on accumulated dispersion. Computer simulation.

reaches approximately 2 ns/nm. Further increase of accumulated dispersion does not lead to increase of the nonlinear noise generated in one span. This result contradicts results reported in [11].

For spans with accumulated dispersion  $> 2$  ns/nm (i.e. all spans except the 1st and the 2nd) the nonlinear coefficient of a single span equals to  $\eta_0 = 14.2 \times 10^{-5} \text{ mW}^{-2}$ .

## 5. Computer simulation

In order to investigate the nature of superlinear accumulation of nonlinear noise in a multi-span line we have performed a computer simulation (numerical modeling).

During the computer simulation, as well as in physical experiments, we have measured the dependence of BER on accumulated dispersion. Results are shown on Fig. 3 (dashed line).

The results of computer simulation correspond well with the experimental data that proves the adequacy of the numerical model and calculation algorithms.

As seen from the dependence on Fig. 3, the nonlinear noise power is not linearly dependent on the value of accumulated dispersion. The minimal nonlinear noise power is generated when the amount of accumulated dispersion at the input of the span equals approximately to  $-200$  ps/nm. With a monotonic increase in the accumulated dispersion, the nonlinear noise power generated in the span is also increasing at first, but then reaches saturation. The saturation level is reached at the dispersion value of approximately 2 ns/nm, which corresponds to dispersion of a 120 km link based on standard telecom fiber with dispersion

coefficient 17 ps/(nm km).

The results of computer simulation were used for calculation of nonlinear power generated in one span and corresponding nonlinear coefficient  $\eta_{NL}$ . We applied here the same method as for analysis of experimental data (see Section 3).

The dependence of nonlinear coefficient on accumulated dispersion in logarithmic representation is shown on Fig. 4. It is basically the same results as on Fig. 3, but represented in other coordinate system. Here we chose the same axes as in [11, figure 11] to simplify the comparison.

## 6. Conclusions

Our experimental researches and computer simulations have confirmed that a communication line model with an additive Gaussian noise is a good approximation for both linear and nonlinear modes of transmission of optical signals in coherent fiber optic links with a large accumulated dispersion. In particular, this model can be used for description of transmission of optical signals in links without dispersion compensation with lengths more than 300 km.

It was shown that increase of a nonlinear noise generated in a span with increasing of accumulated dispersion reaches saturation level at a value of accumulated dispersion of approximately 2 ns/nm. This value corresponds to dispersion of a 120 km link based on standard telecom fiber with dispersion coefficient 17 ps/(nm km). The minimal nonlinear noise power is generated when a value of accumulated dispersion at the input of a span equals approximately to  $-200$  ps/nm.

It was established that the dependence of the total nonlinear noise power on number of spans can be approximated with the power function  $R_{NL} = \zeta P_S^2 N^{1+\varepsilon}$ , where  $\zeta = 14.2 \times 10^{-5} \text{ mW}^{-2}$  and  $\varepsilon = 0.15$ . The coefficient  $\varepsilon$  is possibly conditioned by the correlation of nonlinear noises in different spans, but this hypothesis needs further research.

## References

- [1] A. Splett, C. Kurzke, K. Petermann, Ultimate transmission capacity of amplified optical fiber communication systems taking into account fiber nonlinearities, Proc. ECOC 2 (1993) 41–44.
- [2] X. Chen, W. Shieh, Closed-form expressions for nonlinear transmission performance of densely spaced coherent optical OFDM systems, Opt. Express **18** (18) (2010) 19039–19054.
- [3] D. Rafique, A.D. Ellis, Impact of signal-ASE four-wave mixing on the effectiveness of digital back-propagation in 112 Gb/s PM-QPSK systems, Opt. Express **19** (4) (2011) 3449–3454.
- [4] A. Carena, V. Curri, G. Bosco, P. Poggiolini, F. Forghieri, Modeling of the impact of nonlinear propagation effects in uncompensated optical coherent transmission links, J. Lightwave Technol. **30** (10) (2012) 1524–1539.
- [5] A. Carena, G. Bosco, V. Curri, P. Poggiolini, M.T. Taiba, F. Forghieri, Statistical characterization of PM-QPSK signals after propagation in uncompensated fiber links, Proc. ECOC **P4** (2010) 07.
- [6] P. Poggiolini, The GN model of non-linear propagation in uncompensated coherent optical systems, J. Lightwave Technol. **30** (24) (2012) 3857–3879.
- [7] N.V. Gurkin, O.E. Nanii, A.G. Novikov, S.O. Plaksin, V.N. Treshchikov, R. Ubaidullaev, Nonlinear interference noise in 100-Gbit/s communication lines with the DP-QPSK modulation format, Quantum Electron. **43** (6) (2013) 550–553.
- [8] O.V. Sinkin, J.-X. Cai, D.G. Foursa, H. Zhang, A.N. Pilipetskii, G. Mohs, N.S. Bergano, Scaling of nonlinear impairments in dispersion-uncompensated long-haul transmission, in: Proceedings of the OFC/NFOEC, 2012.
- [9] E. Torrenzo, R. Cigliutti, G. Bosco, A. Carena, V. Curri, P. Poggiolini, A. Nespola, D. Zeolla, F. Forghieri, Experimental validation of an analytical model for nonlinear propagation in uncompensated optical links, in: Proceedings of the ECOC, 2011.
- [10] F. Vacondio, C. Simonneau, L. Lorc, J.-C. Antona, A. Bononi, S. Bigo, Experimental characterization of Gaussian-distributed nonlinear distortions, in: Proceedings of the ECOC, 2011.
- [11] F. Vacondio, O. Rival, C. Simonneau, E. Grellier, A. Bononi, L. Lorc, J.-C. Antona, S. Bigo, On nonlinear distortions of highly dispersive optical coherent systems,

- Opt. Express **22** (2) (2012) 1022–1032.
- [12] A. Bononi, N. Rossi, P. Serena, On the nonlinear threshold versus distance in long-haul highly-dispersive coherent systems, Opt. Express **20** (2012) B204–B216.
- [13] P. Serena, A. Bononi, An alternative approach to the gaussian noise model and its system implications, J. Lightwave Technol. **31** (22) (2013) 3489–3499.
- [14] A. Bononi, P. Serena, N. Rossi, E. Grellier, F. Vacondio, Modeling nonlinearity in coherent transmissions with dominant intrachannel-fourwave-mixing, Opt. Express **20** (7) (2012) 7777–7791.
- [15] A. Mecozzi, R.J. Essiambre, Nonlinear Shannon limit in pseudolinear coherent systems, J. Lightwave Technol. **30** (12) (2012) 2011–2024.
- [16] L. Beygi, E. Agrell, P. Johannisson, M. Karlsson, H. Wymeersch, P. Andrekson, Discrete-time model for uncompensated single-channel fiber-optical links, IEEE Trans. Commun. **60** (11) (2012) 3440–3450.
- [17] G. Bosco, A. Carena, R. Cigliutti, V. Curri, P. Poggiolini, F. Forghieri, Performance prediction for WDM PM-QPSK transmission over uncompensated links, in: Proceedings of the OFC, 2011.
- [18] E. Grellier, A. Bononi, Quality parameter for coherent transmissions with Gaussian-distributed nonlinear noise, Opt. Express **19** (13) (2011) 12781–12788.
- [19] P. Serena, A. Bononi, On the accuracy of the Gaussian nonlinear model for dispersion-unmanaged coherent links, in: Proceedings of the ECOC, 2013.
- [20] R. Dar, M. Feder, A. Mecozzi, M. Shtaif, Properties of nonlinear noise in long, dispersion-uncompensated fiber links, Opt. Express **21** (22) (2013) 25685–25699.
- [21] V.V. Gainov, N.V. Gurkin, S.N. Lukinich, S.G. Akopov, S. Makovejs, S.Y. Ten, O. E. Nanii, V.N. Treshchikov, Record 500 km unrepeated 100 Gb s<sup>-1</sup> transmission, Laser Phys. Lett. **10** (075107) (2013) (4 pp.).
- [22] N.V. Gurkin, V. Mikhailov, O.E. Nanii, A.G. Novikov, V.N. Treshchikov, R. R. Ubaydullaev, Experimental investigation of nonlinear noise in long haul 100 Gb/s DP-QPSK communication systems using real-time DSP, Laser Phys. Lett. **11** (095103) (2014) (4 pp.).
- [23] V.V. Gainov, N.V. Gurkin, S.N. Lukinich, S. Makovejs, S.G. Akopov, S.Y. Ten, O. E. Nanii, V.N. Treshchikov, M.A. Sleptsov, Record 500 km unrepeated 1 Tbit/s (10 × 100G) transmission over an ultra-low loss fiber, Opt. Express **22** (2014) 22308–22313.
- [24] A.A. Redyuk, O.E. Nanii, V.N. Treshchikov, V. Mikhailov, M.P. Fedoruk, 100 Gb/s coherent DWDM system reach extension beyond the limit of electronic dispersion compensation using optical dispersion management, Laser Phys. Lett. **12** (025101) (2015) (5 pp.).